

# Derive Uniform Acceleration Equations

- only valid if the acceleration is uniform

definition:

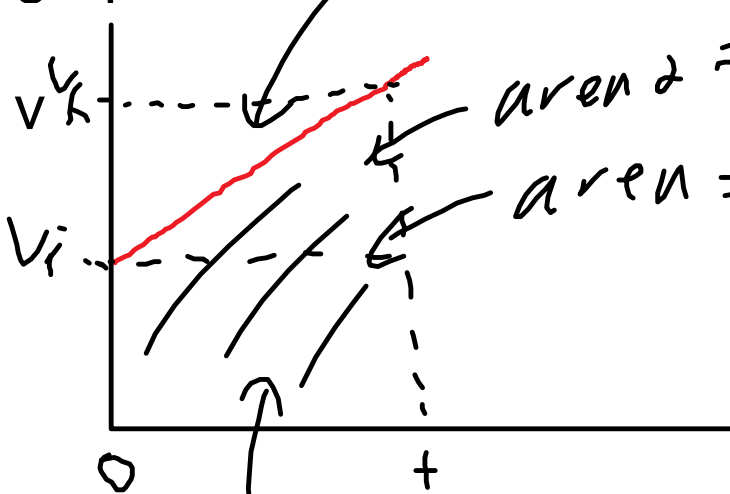
Acceleration,  $a$  - rate of change in velocity

$a = \Delta v / \Delta t$  = slope of the  $v$ - $t$  graph

$$a = (v_f - v_i) / t \quad \text{or} \quad at = v_f - v_i$$

$$v_f = at + v_i$$

graph:



$$\text{slope} = \frac{\text{rise}}{\text{run}} = \frac{v_f - v_i}{t} = a$$

$$\text{area} = \frac{v_f - v_i}{2} t$$

area = displacement,  $d$

$$\text{area 1} = v_i \times t$$

$$\text{total area} = v_i t + \left( \frac{v_f - v_i}{2} t \right)$$

$$= v_i t + \frac{1}{2} v_f t - \frac{1}{2} v_i t$$

$$= \frac{1}{2} v_i t + \frac{1}{2} v_f t$$

$$= \frac{1}{2} (v_i + v_f) t$$

$$d = \frac{1}{2} (v_i + v_f) t$$

eg. A car is moving at 10.0m/s and accelerates uniformly to 16.0 m/s over 3.0 s. After 3.0s it slows uniformly to 8.0 m/s over 4.0 more seconds.

- determine the acceleration when it is speeding up and slowing down.
- determine the displacement of the car.
- graph d-t, v-t

Q9-12 and 13-16 pages 69-72

lab next class - read [labbook p22-23](#)

prepare a data table

eg. A car is moving at 10.0m/s and accelerates uniformly to 16.0 m/s over 3.0 s. After 3.0s it slows uniformly to 8.0 m/s over 4.0 more seconds.

- determine the acceleration when it is speeding up and slowing down.

$$\frac{16 \text{ m/s} - 10 \text{ m/s}}{3.0 \text{ s}} = 2.0 \text{ m/s}^2$$

$$\frac{8.0 \text{ m/s} - 16.0 \text{ m/s}}{4.0 \text{ s}} = -2.0 \text{ m/s}^2$$

\* average acceleration: total change in velocity/total time

$$a = (8 - 10)/7 = -0.2857 = -0.29 \text{ m/s}^2$$

a) determine the displacement of the car.

$$d = \frac{1}{2}(v_i + v_f)t = 0.5 \times (10 + 16) \times 3 = 39 \text{ m}$$

$$0.5 \times (16 + 8) \times 4 = 48 \text{ m}$$

$$\text{total } d = 39 + 48 = 87 \text{ m}$$

average velocity? total d/total time

$$V_{\text{avg}} = 87/7 = 12.4286 = 12 \text{ m/s}$$

a) graph d-t, v-t

90 J  
en 7

... bulas ~ 1

47 m  
at 7 s



a) graph  $a$ ,  $v$ ,  $x$

